

# **Theoretical investigation of the origins of abrupt thermochromism in the polysilanes**

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Values of the conformation-dependent polymer-solvent interaction parameter  $V_D$  have been calculated for some simple polysilane model compounds using quantum-mechanically derived molecular polarizabilities coupled with London's dispersion formula. The value  $V_D = 0.97 \text{ kcal mol}^{-1}$  obtained in the present study for the  $\sigma$ -conjugated polysilanes nearly equals the  $V_D \approx 1.1 \text{ kcal mol}^{-1}$  estimated by Schweizer for the analogous  $\pi$ -conjugated carbon-backbone polymers, assuming similar physical conditions. The present results thus provide theoretical evidence in support of the pertinence of Schweizer's theory of abrupt thermochromism to the polysilanes. The conformational flexibility and versatility of the backbone is much greater for the polysilanes compared with most  $\pi$ -conjugated polymers, hence the conformational 'defect energy'  $\varepsilon$  of the former should be small or even negative. The combination of large  $V<sub>D</sub>$  (favouring the 'ordered' backbone) and small e (favouring the 'disordered' backbone) predicted for the polysilanes would place the critical  $V_B/\varepsilon$  parameter well in excess of the limiting value  $V_D/\varepsilon \ge 0.37$  required for onset of abrupt thermochromism according the Schweizer. The (Austin Model 1) AMl-calculated change in polarizability  $\Delta\alpha$  with respect to backbone rotation  $\phi$  was 0.63  $\rm A^3$  for the model polysilane but only 0.08  $\rm A^3$ for the analogous non-conjugated carbon-backbone model polymer. This substantial difference substantiates the existence of strong coupling between the molecular polarizability and the backbone conformation in the polysilanes. Only the longitudinal polarizability  $\alpha_{xx}$  contributes substantially to  $\Delta \alpha$ , while the transverse polarizabilities  $\alpha_{yy}$  and  $\alpha_{zz}$  essentially combine with no net effect on  $\Delta \alpha$  (i.e.  $\Delta\alpha_{yy} \approx -\Delta\alpha_{zz}$ ). The variation of the calculated band-gap energy  $E_{\rm g}$  with  $\alpha$  for corresponding values of fits a second-order regression curve (correlation coefficient  $r = 0.98$ ). As the silicon backbone approaches an *all-trans* conformation, the highest occupied molecular orbital (HOMO) energy increases while the lowest unoccupied molecular orbital (LUMO) energy decreases to reduce  $E_g$ . This increase in the HOMO energy is balanced by a nearly equal decrease in the HOMO-1 energy; likewise, the decrease in the LUMO energy is balanced by an increase in the LUMO+I energy. Copyright © 1996 Elsevier Science Ltd.

(Keywords: polysilanes; abrupt **thermochromism; interaction parameter)** 

# INTRODUCTION

The polysilanes  $[-SiRR'-]$ , where R and R' can represent a variety of aliphatic and aromatic groups, possess highly interesting physical, chemical and electronic properties of potential use in advanced technologies. (For background and reviews, see refs 1-15.) Some polysilanes have shown promise as u.v. photoresists in microlithography, as radical photoinitiators, as impregnating agents for strengthening ceramics and as precursors of silicon carbide fibres for use in advanced composites. Owing to their  $\sigma$ -conjugated silicon backbone, polysilanes have attracted interest as dopable electrical conductors and semiconductors<sup>10</sup>, as photoconductors<sup> $17-20$ </sup>, as charge-transport materials in electrophotography<sup>21-23</sup> and as non-linear optical materials $^{24-30}$ .

An interesting feature of the polysilanes is their unusual electronic structure. All substituted silane high polymers absorb strongly in the u.v. at 300-400nm. Their absorption characteristics depend on the molecular weight of the polymer and on the conformation of the silicon backbone; consequently, many polysilanes are thermochromic both in solution and in the solid state  $1-15$ . For example, the homologous series of symmetrically substituted poly(di-n-alkylsilane)s  $[-SiR_2-]$ , from  $R =$  methyl to  $R =$  n-octyl, exhibit a wide range of structural and thermochromic properties *(Table 1).* 

A most unusual phenomenon exhibited by some polysilanes is *abrupt thermochromism,* characterized by a dramatic (ca. 60 nm) and reversible bathocromic shift in the absorption maximum  $\lambda_{\text{max}}$  as the temperature falls below a critical transition temperature  $T_c$ . (The adjective 'abrupt' is meant to convey that this thermochromic transition is discontinuous with temperature and thus eludes interpretation by statistical-based treatments such as rotational isomeric state (RIS) theory $^{8,9}$ .) A large body of experimental and theoretical evidence attributes these sharp red-blue thermochromic transitions to associated 'order-disorder' conformational transitions along the silicon backbone. Specifically, the low-temperature 'ordered' structure responsible for the red-shifted  $\lambda_{\text{max}}$  has been described in terms of long runs of the *all-trans* (or nearly *all-trans)* backbone

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Polymer	R	Solid-state conformation <sup><i>b</i></sup>	Abrupt thermochromism?		
			In solid state	In solution	Ref.
<b>PDMS</b>	n-methyl	trans	no	not sol.	31
<b>PDES</b>	n-ethyl	near <i>trans</i>	no	no	32
<b>PDPrS</b>	n-propyl	near trans	no	no	32
<b>PDBS</b>	n-butyl	$7/3$ helix	no	yes $(-48^{\circ}C)$	33
<b>PDPS</b>	n-pentyl	$7/3$ helix	no	yes $(-33^{\circ}C)$	33, 34
<b>PDHS</b>	n-hexyl	trans	yes $(42^{\circ}C)$	yes $(-28^{\circ}C)$	35
<b>PDOS</b>	n-octyl	trans	yes $(-19^{\circ}C)$	yes $(-35^{\circ}C)$	36
<b>PDTDS</b>	n-tetradecyl	TGTG'	yes $(54^{\circ}C)$		37

**Table 1** Conformational and thermochromic behaviour of some poly(di-n-alkylsilanes)  $[-SiB_2-1]^d$ 

General information has been taken from refs  $1-15$  and  $31-42$ . Particular references to individual polymers are also quoted

Observed at ambient temperatures (below  $T<sub>c</sub>$ ) and pressures

conformation. These *all-trans* sequences extend the mean conjugation length of the  $\sigma$ -conjugated silicon backbone, thereby shifting absorption to the red. The 'disordered' structure is viewed as a conformationally extended but more disordered backbone containing kinks that disrupt the long runs of all-*trans* backbone and thus shift  $\lambda_{\text{max}}$  to the blue.

The molecular basis of these order-disorder transitions, particularly the solution phenomena, has been the subject of intense scrutiny  $\mathbb{R}^n$ . A salient question concerns the precise mechanism by which the silicon backbone can suddenly and reversibly interconvert between the disordered and ordered forms over a span of typically only  $1-2$ °C. Based on theoretical studies carried out in this laboratory<sup>43–54</sup> and by others<sup>55–69</sup>, as well as on experimental data  $1 - 13,31 - 37$ , ample evidence confirms that the silicon backbone is inherently flexible and capable of populating helical (i.e. *non-trans)*  conformations. Some polysilanes are known to adopt such helical backbones in the solid state *(Table 1).* Hence, a unique driving force must be operative to stabilize the *all-trans* (or nearly *all-trans)* backbone conformation. In this regard, two opposing mechanisms have been suggested: (1) the 'single chain' model, which basically derives this driving force from the inherent  $\sigma$ -delocalized electronic structure of the polysilane chain<sup>38</sup>; and (2) the 'aggregation' model, whereby intermolecular (and perhaps intramolecular) side chain $\cdots$ side chain interactions promote alignment of the all-*trans* backbone<sup>39-42</sup>.

In recent years, Schweizer has proposed an interesting theory in support of the 'single chain' model  $V^{p-12}$ . According to his theory, abrupt thermochromism can be induced by a unique conformation-dependent polymer-solvent interaction associated with conjugated polymers. In the polysilanes, this interaction arises from the dispersion-like attractions between the  $\sigma$ -delocalized electrons of the silicon backbone and the polarizable local medium—which can be solvent molecules, neighbouring chains, or even the polymer's own side chains. Schweizer formulated his theory in terms of the ratio  $V_{\rm D}/\epsilon$  where  $V_{\rm D}$  is the conformation-dependent dispersion energy per backbone bond or atom and  $\epsilon$  is the 'defect energy' representing the free-energy cost to rotate the bond in question from *trans* to the 'defect' conformation. The parameter  $V_D/\epsilon$  is conveniently employed as a guide for predicting whether the

thermochromic transition will be continuous or abrupt. Specifically, abrupt thermochromism increases in likelihood with increasing  $V_{\rm D}/\epsilon$  and, at least for the  $\pi$ -conjugated polymers, appears to satisfy the limiting condition  $V_D/\epsilon \ge 0.37$ . For the polysilanes and most other conjugated polymers, the electron delocalization and, in turn, longitudinal polarizability  $\alpha_{xx}$  are highly dependent on the backbone conformation and will approach a maximum at *all-trans.* Since dispersion forces depend in general on the polarizability  $\alpha$  of the interacting atoms or groups, the contribution of this special conformation-dependent dispersion<br>energy will stabilize the all-trans backbone will stabilize the all-*trans* backbone conformation.

The polysilanes represent excellent candidates to explore the relationship between Schweizer's theory and abrupt thermochromism. Their  $\sigma$ -delocalized electronic structure should translate to large values of  $V_{\text{D}}$ , and the inherent conformational flexibility of the Si-Si bond implies small values of  $\epsilon$ . This combination suggests that the limiting condition  $V_D/\epsilon \geq 0.37$  for onset of abrupt thermochromism should be easily satisfied by the polysilanes. Most  $\pi$ -conjugated polymers (e.g. polyacetylene) are conformationally inflexible and strongly prefer the *all-trans* backbone or nearly so. The polysilanes, by contrast, are conformationally more versatile and capable for populating the same *non-trans*  helical backbone conformations *(Table 1)* that are associated with the conformational 'defect' parameter  $\epsilon$ . As a consequence, the conformational defect energy  $\epsilon$ is likely to be small or even negative for many polysilanes. This combination of large  $V<sub>D</sub>$  and small (or negative)  $\epsilon$  fulfils the conditions of Schweizer's theory, according to which a pseudo-first-order phase transition between the ordered and disordered phase requires a bimodal conformational free-energy surface afforded by a large  $V<sub>D</sub>$  (favourable to *trans*) and a small or negative  $\epsilon$  (unfavourable to *trans*).

The merit of Schweizer's theory in explaining the observed order-disorder transitions in the polysilanes and other conjugated polymers depends in part on the magnitude of  $V<sub>D</sub>$ . Combining theoretical and experimental data with a general dispersion expression, Schweizer obtained  $V_D \approx 1.1 \text{ kcal mol}^{-1}$  as a reasonable estimate for the  $\pi$ -conjugated polyenes. Taking  $\epsilon \approx 1$  kcalmol<sup>-1</sup> from the literature, he concluded that

 $V_{\rm D}/\epsilon \approx 1.1$  exceeds the threshold value of 0.37 required for onset of the abrupt order-disorder transition<sup>70-72</sup>.

In the present study, the relevance of Schweizer's theory to the polarizability  $\alpha$  were derived quantummechanically for model compounds of the simple polysilanes  $[-SiH<sub>2</sub>-]$  (polysilane, PS) and  $[-Si(CH)<sub>3</sub>)<sub>2</sub>-]$ (polydimethylsilane, PDMS) as a function of rotation  $\phi$ about an internal Si-Si bond. The variation in  $\alpha$  (and  $\alpha_{xx}$  in particular) with  $\phi$  is substantially larger for the polysilanes than for the analogous non-conjugated carbon-backbone polymer. Specifically, the present results reveal that  $\Delta \alpha$ , defined as the maximum change in  $\alpha$  with  $\phi$ , is 0.6 Å<sup>3</sup> for H-[SiH<sub>2</sub>]<sub>10</sub>-H but only  $0.08\text{ Å}^3$  for H-[CH<sub>2</sub>]<sub>10</sub>-H. This difference is consistent with the notion that conjugated polymers uniquely exhibit strong coupling between the backbone conformation and the extent of electron delocalization. The quantity  $\Delta \alpha$ , which can be ascribed to a single atom in the rotated bond, represents the maximum enhancement in the polarizability of the atom resulting from electron delocalization.

 $V_{\rm D}$  was calculated for the polysilanes from  $\Delta \alpha_{\rm Si}$  and the polarizability  $\alpha_s$  of the solvent particles using the Slater-Kirkwood formula  $3-15$  in conjunction with the classical London dispersion expression  $\mathbb{S}^{7,77}$ . A crude estimate of  $V_D = 0.97$  kcalmol<sup>-1</sup> was obtained based on a simple representation of the 'solvent' in the vicinity of the subject Si atom. This value is nearly identical to the  $V_{\rm D} \cong 1.1$  kcal mol<sup>-1</sup> obtained by Schweizer for polyenes under similar physical conditions<sup>70-72</sup>. Therefore, the present work supports the applicability of Schweizer's 'single chain' theory to the polysilanes in that  $V_D$  is sufficiently large to stabilize the *all-trans* backbone conformation and thereby promote abrupt thermochromism. At the same time, the role of side chain... side chain aggregation and precipitation in this phenomenon cannot be ruled out and many indeed function independently of 'single chain' effects.

#### COMPUTATIONAL METHODOLOGY

The two simple polysilanes  $[-SiH_2-]$  (PS) and  $[-Si(CH_3)_2-]$ (PDMS), represented respectively by the oligomeric model compounds  $H-[SiH<sub>2</sub>]<sub>n</sub>-H$  (where  $n = 5$ , 10) and  $CH_3-[Si(CH_3)_2]_5-CH_3$ , were chosen for the present calculations. The choice of these simple structures, devoid of long side chains, afforded computational efficiency while at the same time focused attention on the inherent properties of the silicon backbone.

Construction, visualization and manipulation of all molecular structures were carried out using Biosym's molecular modelling program *Insight. (Insight,* a molecular modelling program, and *DMol,* a quantummechanical program based on density functional theory, are products of Biosym Technologies, San Diego, CA.) For the two PS model compounds, PS-5 and PS-10, full geometry optimization via energy minimization was performed on all conformations using Biosym's *DMol* module. *DMol* utilizes numerical atomic-orbital basis sets to calculate the variational selfconsistent solutions to the density function theory (DFT) equations. The most rigorous *(DNP)* basis set and mesh parameters and the maximum number of mesh points available in *DMol* were utilized for this study. The *DNP* 

basis set employs double numeric basis functions and polarization functions to define the atomic orbitals.

For the PDMS model compound PDMS-5, the all*trans* form was full geometry-optimized using *DMol* in order to obtain reasonable geometric parameters, viz.  $Si-Si = 2.33 \text{ Å}, \text{Si}-C = 1.83 \text{ Å}, C-H = 1.09 \text{ Å}$  and Si- $Si-Si = 111^{\circ}$ . The computational demands of the DFT calculations precluded full geometry optimization for the other conformers. Instead, the geometric parameters were fixed to those calculated for the *all-trans* form while the torsion angle  $\phi$  was incremented.

At the time of the present study, calculations of molecular polarizability were not feasible using *DMol.*  Therefore, the molecular polarizabilities for each of the previously *DMol-optimized* geometries were computed using the Austin Model 1  $(AM1)^{78}$  Hamiltonian coupled with the finite-field methodology accessed through *Insight's Mopac* module. Values of the average molecular polarizability  $\alpha$  and its components  $\alpha_{xx}$ ,  $\alpha_{yy}$  and  $\alpha_{zz}$ (where  $\alpha = (\alpha_{xx} + \alpha_{yy} + \alpha_{zz})/3$ ) were generated *versus* rotation  $\phi$  about an internal Si-Si bond *(Figure 1)* varied from *trans* ( $\phi = 180^{\circ}$ ) to *cis* (= 0°) in increments of 15°. The energies of the electronic band gap  $E_{\rm g} = E_{\rm LUMO} - E_{\rm HOMO}$  and of the six frontier molecular orbitals HOMO-2, HOMO-l, HOMO, LUMO, LUMO+I, and LUMO+2 were also extracted from the *Mopac* AM1 output for use in interpreting the polarizability data. The finite-field methodology<sup>7</sup> employed in *Mopac* solves the molecular wave function  $\psi$  as a function of an external electric field F. From the wave function  $\psi(F)$ , both the field-dependent molecular energy  $E(F)$  and dipole moment  $\mu(F)$  can then be used to calculate  $\alpha$ .

To calculate values of  $\alpha$  for these systems with absolute accuracy would surely require application of rigorous *ab initio* theory with large basis sets inclusive of  $\frac{1}{2}$  correlation<sup>80</sup>. Such calculations would have overwhelmed the available computational resources and, in fact, would have exceeded the primary objectives of the present study, which was to evaluate Schweizer's theory qualitatively and to identify general trends in  $\alpha$  with respect to  $\phi$ . The semiempirical AM1 method offers a feasible alternative to *ab initio* approaches for the present purposes owing to its computational efficiency and its demonstrated ability to capture many of the essential electronic features of molecules and polymers<sup>81,82</sup>. The ability of AM1 (coupled with the finite-field methodology) to discern the sharp differences between PS-10 and PC-10 with regard to their  $\alpha$  *versus*  $\phi$  profiles builds confidence in the validity of the present approach.

A complete set of  $\alpha$  *versus*  $\phi$  values was calculated for three specific polysilane oligomers:  $H$ -[Si $H_2$ ]<sub>5</sub>-H (PS-5),  $H-[SiH<sub>2</sub>]<sub>10</sub>-H$  (PS-10) and  $CH<sub>3</sub>-[Si(CH<sub>3</sub>)<sub>2</sub>]<sub>5</sub>-CH3$ (PDMS-5). PS-5 and PDMS-5 each contained four Si-Si bonds and two Si-Si-Si-Si torsion angles, of which one torsion angle was taken as  $\phi$  while the other was



Figure 1 Silicon backbone of the  $H-[SiH<sub>2</sub>]_{10}-H$  (PS-10) model compound, indicating rotation  $\phi$  about the central Si-Si bond

held at *trans*. **PS-10** contains nine Si-Si bonds and seven 0.7 Si-Si-Si-Si torsion angles, of which the central torsion angle (i.e. the fifth Si-Si bond) was taken as  $\phi$  while the remaining six torison angles were held in the *trans*  conformation *(Figure 1).* The conformational defect in PS-10 is straddled by pentameric silicon sequences, which are sufficiently long to mimic the chain-like features of the polysilanes.  $\frac{1}{2}$  0.5

#### RESULTS AND DISCUSSION

# *Polarizabilities* versus

The calculated values of  $\alpha$  *versus*  $\phi$  have been tabulated for the polysilane model compounds PS-5, PS-10 and PDMS-5 *(Table 2).* For comparison, *Table 2*  also includes corresponding values for the non-conjugated carbon-backbone model compound  $H-(CH<sub>2</sub>)_{10}$ H (PC-10) analogous to PS-10. The results show that  $\Delta \alpha = \alpha_{180^\circ} - \alpha_{0^\circ}$  is substantially larger for the three polysilane model compounds than for PC-10. Specifically,  $\Delta \alpha$  is 0.63 Å<sup>3</sup> for PS-10 but only 0.08 Å<sup>3</sup> for PC-10. This result substantiates the existence of strong coupling between the molecular polarizability and backbone conformation in the polysilanes.

It is convenient to normalize  $\alpha$  by defining the quantity  $\alpha' = \alpha - \alpha_0$ , where  $\alpha$  is the AM1-calculated molecular polarizability and  $\alpha_0$  is the polarizability of the  $\phi = 0^\circ$  $(cis)$  conformation for a given polymer. Plotting  $\alpha'$  *versus*  $\phi$  for PS-5, PS-10 and PDMS-5 *(Figure 2)*, the curves reveal that  $\alpha'$  (and, hence,  $\alpha$ ) diminishes gradually, at first sharply, as  $\phi$  deviated from  $\phi = 180^{\circ}$  *(trans)*. For PS-10, for example,  $\alpha'$  decreases from its maximum value of 0.63 Å<sup>3</sup> at  $\phi = 180^\circ$  by approximately 1.3% at 165°, 17% at  $150^\circ$  and  $81\%$  at  $90^\circ$ . Similar trends were obtained for PS-5 and PDMS-5.

It is apparent from *Table 2* and *Figure 2* that  $\Delta \alpha$  is roughly twice as large for PS-10 as for PS-5 and PDMS-5, a result that is consistent with the relative lengths of their respective silicon backbones. As expected, the magnitude of  $\Delta\alpha$  correlates with the length of the all*trans* backbone that is being disrupted by the conformational defect. Since  $V_{\text{D}}$  is a function of  $\Delta \alpha$  through the Slater-Kirkwood formula *(vide infra),* the magnitude of  $V<sub>D</sub>$  will likewise depend on the lengths of all-*trans* 

**Table 2** Calculated values of  $\alpha$  *versus*  $\phi$  for PS-5, PS-10 PDMS-5 and PC-10

	Average polarizabilities $(\mathring{A}^3)$					
$\phi$ (deg)	<b>PS-5</b>	$PS-10$	PDMS-5	$PC-10$		
180	16.8580	36.2646	24.4833	12.0830		
165	16.8491	36.2562	24.4646	12.0750		
150	16.8189	36.1556	24.4184	12.0652		
135	16.7397	36.0471	24.3719	12.0474		
120	16.6840	35.9339	24.3295	12.0319		
105	16.6398	35.8344	24.2814	12.0272		
90	16.6084	35.7581	24.2445	12.0343		
75	16.5854	35.7068	24.2285	12.0491		
60	16.5761	35.6788	24.2297	12.0609		
45	16.5425	35.6682	24.1983	12.0543		
30	16.5757	35.6610	24.1315	12.0305		
15	16.5531	35.6464	24.1228	12.0094		
0	16.4874	35.6366	24.1135	12.0035		
$\Delta \alpha$	0.3706	0.6280	0.3698	0.0795		



**Figure 2** Calculated values of  $\alpha'$  *versus*  $\phi$  for the polysilane model compounds PS-5, PS-10 and PDMS-5

backbone that straddle the conformational defect. The present calculation of  $V_D$  pertains to PS-10, in which case the decameric *all-trans* silicon backbone is essentially being divided by the conformational defect into two pentameric *all-trans* subunits. This scenario might represent a typical case occurring in the polymer.

#### *Estimation of*  $V_D$  *for the polysilanes*

Schweizer deduced  $V_D \approx 1.1 \text{ kcal mol}^{-1}$  for a polyene in dilute solution of a typical non-polar organic solvent<sup> $\sigma$ -12. In the present application,  $V_D$  was estimated</sup> for the polysilanes under similar conditions using the data calculated above for PS-10. Adopting the form of the London dispersion equation<sup>'0,''</sup>  $E_{\text{diss}} = c_{ii}/R^{\circ}$ , an expression for  $\bar{V}_{\rm D}$  can be written

$$
V_{\rm D} = -\sum_{z} [(-c_{ij}/R^6)_{trans} - (c_{ij}/R^6)_{non-trans\,\,\text{defect}}] \quad (1)
$$

where  $i$  refers to the Si atom in question and  $j$  refers to the atoms comprising the local solvent molecules, respectively. The summation is taken over the number of solvent molecules  $Z$  in the vicinity of the subject bond. (The leading minus sign in equation (1) has been added since an attractive  $\bar{V}_{\text{D}}$  energy is defined as positive.) Equation (1) states that  $V<sub>D</sub>$  is calculated as a difference in polymer-solvent dispersion energy between the all-trans conformation and the *non-trans* (i.e. defect-containing) conformation. The required  $c_{ij}$  parameters were deduced from the Slater-Kirkwood formula<sup>73-75</sup>:

$$
c_{ij} = 360.0 \alpha_i \alpha_j / [(\alpha_i / N_i)^{1/2} + (\alpha_j / N_i)^{1/2}] \tag{2}
$$

where  $\alpha_i$  and  $\alpha_i$  are, respectively, the polarizabilities of the Si atom and of the atoms comprising the solvent molecules. The parameters  $N_i$  and  $N_j$  represent the effective number of outer-shell electrons  $N_{\text{eff}}$  in atoms *i* and *j*. The factor 360.0 produces  $c_{ij}$  in kcal  $A^{\circ}$  mol<sup>-1</sup> for  $\alpha$  expressed in  $A^3$ .

Values of  $(c_{ij})_{trans}$  and  $(c_{ij})_{non-trans\ defect}$  required for equation (1) were computed by inserting the appropriate value of  $\alpha_i$  into equation (2) for the type of Si atom in each case. For  $(c_{ij})$ <sub>non-trans</sub> defect,  $\alpha_i$  was assigned the standard value of  $2.\dot{8}A^3$  for a typical Si atom devoid of any extra delocalization effects<sup>43,45,54,83</sup>. For  $(c_{ij})_{trans}$ , this  $\alpha_i$  value is augmented by  $\Delta\alpha$  to reflect the enhancement in polarizability due to electron delocalization. The value  $\Delta \alpha = 0.63 \text{ Å}^3$  calculated for PS-10 *(Table 2)* was taken as a reasonable estimate for this quantity. Accordingly, the augmented value of  $\alpha_i$  associated with  $(c_{ij})_{trans}$  is 3.43  $\mathbf{A}^3$ . Following Schweizer<sup>70-72</sup>, it was assumed that the maximum change in polarizability of PS-10 can be assigned to a single Si atom in the rotating backbone bond.

To estimate  $V_D$  for the polyenes, Schweizer assumed a first solvent shell of  $Z = 8$  molecules (each with  $\alpha_{\rm s} \sim 10.4$  A<sup>3</sup>) located at a distance  $R = 4.5$  A from the polyene CH group under consideration  $\mathcal{P}^{-1/2}$ . In the present derivation of  $V<sub>D</sub>$ , equations (1) and (2) have been formulated in terms of the atomic polarizabilities  $\alpha_i$ of the atom composing the solvent molecules. Organic solvent molecules like hexane, benzene and toluene contain 6-7 carbon atoms, so  $Z = 8$  solvent molecules would yield approximately  $8 \times 6 = 48$  highly polarizable carbon atoms. Each of these carbon atoms was assigned the parameters  $\alpha_i = 0.93 \text{ A}^3$  and  $N_i = 5.0^{83}$ . The corresponding parameters for the Si atom in PS-10 are  $N_i \approx 13$  and either  $\alpha_i = 3.43 \text{ A}^3$  or 2.8 A<sup>3</sup> depending on whether the electron delocalization along the silicon backbone is included or not.

Assuming that each solvent atom is located an average distance  $R$  from the Si atom, equation (1) can be simplified by factorizing out the variable  $R$  to give:

$$
V_{\mathbf{D}} = -(1/R^6) Z N_{\mathbf{a}} [(-c_{ij})_{trans} - (-c_{ij})_{\text{non-trans defect}}] \quad (3)
$$

where Z is the number of solvent molecules and  $N_a$  is the number of polarizable (carbon) atoms in each solvent molecule. The appropriate values of  $\alpha_i$ ,  $\alpha_j$ ,  $N_i$ and  $N_i$  were inserted into equation (2) to obtain  $(c_{ij})_{trams} = 1215$  kcal A<sup>o</sup> mol<sup>-1</sup> and  $(c_{ij})_{non-trans\ defect} = 1047$ kcal  $A^{\circ}$  mol<sup>-1</sup>, which, in turn, were inserted into equation (3) to obtain values for  $V<sub>D</sub>$ .  $V<sub>D</sub>$  is strongly dependent on R, as illustrated by a plot  $V_D$  versus R based on equation (3) for the case  $Z = 8$  and  $N_a = 6$  (Figure 3). For the value  $R = 4.5$ A adopted by Schweizer, equation (3) yields  $V_D = 0.97$  kcal mol<sup>-1</sup> for the polysilanes. Although these calculations are admittedly crude, they provide evidence that  $V<sub>D</sub>$  may be sufficiently large in the polysilanes to support Schweizer's theory of abrupt thermochromism based on solvent-induced conformational changes of the polymer backbone.

#### *Component polarizabilities* versus  $\phi$

The variation of the component polarizabilities  $\alpha_{xx}$ ,  $\alpha_{yy}$  and  $\alpha_{zz}$  with  $\phi$ , as plotted for PS-10 in *Figure 4*, reveals that the sum of the transverse components  $\alpha_{\nu\nu}$ 



**Figure 3** Plot of  $V<sub>D</sub>$  versus R based on equation (3) for the case  $Z = 8$ and  $N_a = 6$ 



**Figure 4** Calculated values of the longitudinal polarizability  $\alpha_{xx}$  and the transverse polarizabilities  $\alpha_{yy}$  and  $\alpha_{zz}$  versus  $\phi$  for PS-10

and  $\alpha_{zz}$  is very nearly constant (i.e.  $\alpha_{yy} + \alpha_{zz} \approx$  constant). This relationship implies the  $\Delta \alpha_{yy} \cong -\Delta \alpha_{zz}$ ; therefore the changes in the transverse polarizabilities with  $\phi$ essentially cancel out. Only the longitudinal component  $\alpha_{xx}$  contributes substantially to the variation of  $\alpha$  with  $\phi$ . Since  $\Delta \alpha = (\Delta \alpha_{xx} + \Delta \alpha_{yy} + \Delta \alpha_{zz})/3$ , it follows that  $\Delta \alpha \cong \Delta \alpha_{xx}/3$  in the present case.

Values of  $\alpha_{xx}$  are nearly double those of  $\alpha_{yy}$  or  $\alpha_{zz}$ *(Figure 4).* This result is as expected since the molecular polarizability will be significantly larger parallel than perpendicular to the chain direction. The  $\alpha_{xx}$  per SiH<sub>2</sub> unit is about 3.63  $\AA^3$  (or 31 a.u.) according to AM1 for PS-10 in the *all-trans* conformation. This compares reasonably well with the range of STO-3G (Slater-type orbitals, three Gaussians) values ( $\approx$  32 a.u.) reported by Kirtman and  $Hasan<sup>80</sup>$ . Both AM1 and STO-3G underestimate the 6-31G (plus diffuse functions) values reported by the same authors. However, use of AM1 was consistent with the major goal of the present study, which was to recognize trends rather than to calculate  $\alpha$ with absolute numerical accuracy.

#### *Polysilane electronic structure*

An increase in electron delocalization, as found for the polysilanes and other conjugated polymers as the backbone approaches *all-trans,* is expected to cause the molecular polarizability  $\alpha$  to increase and the electronic band-gap energy  $E_{\rm g}$  (i.e.  $E_{\rm LUMO} - E_{\rm HOMO}$ ) to decrease. Plots of the AM1-calculated values of  $E<sub>g</sub>$  *versus*  $\phi$  *(Figure* 5) for PS-5, PS-10 and PDMS-5 confirm that  $E_g$ decreases monotonically with increasing  $\phi$  to a minimum at *trans* ( $\phi = 180^{\circ}$ ). A plot of  $E_{\rm g}$  *versus*  $\alpha$  for corresponding values of  $\phi$  yielded a strong secondorder fit with correlation coefficient  $r = 0.98$  (inset to *Figure 5).* 

The AM<sub>1</sub>-calculated energies of the six frontier orbitals HOMO-2, HOMO-l, HOMO, LUMO, LUMO+I and LUMO+2 for PS-10 are plotted *versus*   $\phi$  in *Figure 6.* Consistent with the  $E_g$  *versus*  $\phi$  data plotted in *Figure 5,* the HOMO energy increases and the LUMO energy decreases as  $\phi$  approaches 180°. The HOMO energy changes somewhat more than the LUMO energy, suggesting that the HOMO orbitals are perturbed more so by changes in the backbone conformation. The variations in energy of the HOMO and LUMO with  $\phi$ 



**Figure 5** AM1-calculated values of the electronic band-gap energy  $E_g$ *versus*  $\phi$  *for PS-5, PS-10 and PDMS-5. Inset: plot of*  $E_{\rm g}$  *versus*  $\alpha$  *at* corresponding values of  $\phi$ . The curve shows a second-order regression fit



**Figure 6**  Energies of the frontier molecular orbitals HOMO-2,  $HOMO-1$ ,  $HOMO$ , LUMO, LUMO+1 and LUMO+2 *versus*  $\phi$ , as calcuated by AM1

are strongly correlated with those of the respective penultimate orbitals HOMO-1 and LUMO+I. As the HOMO is destabilized with increasing  $\phi$ , the HOMO-1 is stabilized by almost an equal amount; likewise, as the LUMO is stabilized with increasing  $\phi$ , the LUMO+1 is destabilized almost equally. In contrast, the HOMO-2 and LUMO+2 orbitals remain almost unperturbed by variations in  $\phi$ . This general behaviour of the frontier orbitals conveys the sense that electron delocalization is achieved by donation from the HOMO into the LUMO.

## CONCLUDING REMARKS

Perhaps the most thoroughly investigated polysilanes from the standpoint of thermochromism are the homologous series of symmetrically substituted polysilanes  $[-SiR_2-]$ , particularly PDBS  $(R = n$ -butyl), PDPS  $(R = n$ -pentyl) and PDHS  $(R = n$ -hexyl). Despite the similarity of their molecular structures, PDBS, PDPS and PDHS exhibit significant differences with respect to their conformational preferences and thermochromic behaviour *(Table 1).* In the solid state, PDHS adopts an *all-trans* backbone conformation and exhibits abrupt thermochromism; PDBS and PDPS adopt a 7/3 helical backbone conformation and do not exhibit abrupt thermochromism $33-35$ . (Evidence suggests that the all*trans* backbone is induced by attractive interchain side chain...side chain interactions, which are stronger for PDHS than for PDBS and PDPS.) The clear implication drawn from these comparisons is that the *all-trans*  backbone plays an instrumental role in polysilane abrupt thermochromism. There appears to be general agreement that the long runs of *all-trans* backbone are responsible for the red-shifted  $\lambda_{\text{max}}$  observed below  $T_c$ . Accordingly, the sudden disruption of these *all-trans*  sequences at  $T_c$  causes  $\lambda_{\text{max}}$  to shift to the blue. This interpretation is largely supported by a significant body of theoretical and experimental data on a wide range of polysilanes $1-15$ .

The controversy over the molecular origins of abrupt thermochromism in the polysilanes has centred largely on the thermochromisms of PDBS, PDPS and PDHS in dilute solution. Remarkably, all three polysilanes exhibit abrupt thermochromism in dilute solution *(Table 1)*<sup>39-4</sup> The immediate question that arises relates to the backbone conformation below  $T_c$ , which, according to the above explanation of the solid-state data, is *all-trans*  or nearly so. The crux of this issue deals with finding a mechanism by which PDBS, PDPS and PDHS can adopt this conformation. According to the solid-state data, the *all-trans* backbone is hardly that preferred by PDBS and PDPS and is adopted by PDHS only through the action of interchain forces that presumably are absent in dilute solution. Both the 'aggregation' model  $3^{3-42}$  and the 'single chain' model<sup>38,70–72</sup> attempt to provide the mechanism by which the *all-trans* backbone in PDBS, PDPS and PDHS (and other polysilanes) is stabilized in solution below  $T_c$ .

The 'aggregation' model maintains the primacy of side  $chain \cdot$  side chain interactions to explain both the solidstate and dilute-solution phenomena. In the solid state, these interchain interactions promote crystallization of the side-chain substructure below  $T_c$ , which locks in the all-*trans* backbone responsible for the red-shifted  $\lambda_{\text{max}}$ . This substructure abruptly 'melts' at  $T_c$ , thereby releasing the backbone to adopt the disordered form responsible for the blue-shifted  $\lambda_{\text{max}}$ . In dilute solution, side chain...side chain interactions within a single chain may stimulate at low temperatures a process described as 39&~2 intramolecular polymer collapse , which induces adoption of the *all-trans* backbone. This 'seed' chain may then template the aggregation of other chains also in the *all-trans* backbone conformation.

The alternative 'single chain' or 'rod-to-coil' model seeks to explain the same phenomena in terms of the intrinsic electron delocalization in conjugated polymers, which should act to stabilize the *all-trans* backbone conformation $1 - 15,38,70 - 72$ . Schweizer's theory provides a cogent argument in favour of the 'single chain' model and establishes a feasible mechanism by which the all*trans* backbone conformation is accessible to PDBS, PDPS and PDHS (and other polysilanes). The 'single chain' model obviates the need for chain...chain interactions, and hence it is especially pertinent to the situation found in dilute solution. On the other hand, the 'aggregation' model provides a lucid picture of circumstances in the solid state.

Consistent with Schweizer's theory, the present calculations suggest that the magnitude of  $V<sub>D</sub>$  for the polysilanes is sufficiently large to stabilize the *all-trans*  backbone conformation. The size of the rotational barriers in the polysilanes is highly dependent on the type, length and symmetry of the side chain R; hence the value of  $\varepsilon$  will vary considerably from one polysilane to another. For this reason, a direct calculation of Schweizer's  $V_D/\varepsilon$  parameter has not been attempted here. Compared with typical  $\pi$ -conjugated polymers, polysilanes can more easily populate helical (i.e. non*trans)* backbone conformations. This increased accessibility to *non-trans* backbone conformations implies small or even negative values of  $\varepsilon$ . As a consequence,  $V_{\rm D}/\varepsilon$  is likely to be larger for the polysilanes than for the  $\pi$ -conjugated polymers considered by Schweizer in his analysis<sup>70-72</sup>. It is worth noting that a recent experimental study on the thermochromism of a series of unsymmetrically substituted poly(n-alkylmethylsilane)s has provided additional support for Schweizer's model<sup>84</sup>.

Although applicable to all polysilanes, Schweizer's theory of the 'single chain' model may be difficult to reconcile with the absence of abrupt thermochromism observed for some polysilanes with branched-chain substituents (e.g. poly(di-4-methylpentylsilane))<sup>40</sup>. One would not expect branching to impair abrupt thermochromism within the scheme of a 'single chain' model. On the other hand, this behaviour is consistent with the 'aggregation' model insofar as side-chain branching could thwart the formation of intramolecular and/or intermolecular aggregates. These apparent inconsistencies suggest that the 'aggregation' model of abrupt thermochromism cannot be ruled out. This particularly applies to the abrupt thermochromism observed for some polysilanes in the solid state  $(Table 1)^{1-15}$ 

The magnitude of  $\Delta \alpha$  and, correspondingly,  $V_D$ depends on the specific conformation of the Si-Si bonds astride the Si-Si bond containing the defect. If one *non-trans* defect breaks an otherwise long *all-trans*  sequence, that *non-trans* defect would experience the full magnitude of  $V_D$  calculated in the present study. If, instead, this *non-trans* defect breaks a shorter *all-trans*  sequence, the operative magnitude of  $V_D$  would be something less than this upper limit. Thus, each and every Si-Si bond along the polysilane possesses a unique magnitude of  $V_D$ ;  $V_D$  is, in turn, a dynamic variable of the backbone conformation astride the Si-Si bond in question.

The present study computed  $\Delta\alpha$  and  $V_D$  by arbitrarily choosing the *cis* conformation ( $\phi = 0^{\circ}$ ) as the defect angle. The *cis* conformation will be energetically unfavourable for all substituted polysilanes, and consequently the occurrence of such a defect is highly unlikely in reality. The primary reason for choosing *cis* (i.e. the most extreme defect) was to determine whether the maximum values for  $\Delta \alpha$  and  $V_D$  either supported or refuted Schweizer's model. The present results *(Figure 2)*  reveal that the  $\alpha$  *versus*  $\phi$  curve for the polysilanes falls off sharply between  $\phi = 180^\circ$  *(trans)* and  $\phi = 90^\circ$ , then only slowly between  $\phi = 90^\circ$  and  $\phi = 0^\circ$  *(cis)*. Selecting a defect angle in the vicinity of  $\phi = 90^{\circ}$  would still have captured almost the full magnitude of  $\Delta\alpha$  and  $V_D$ . In any case, it should not be construed that the *cis* conformation was adopted as the defect structure due to any special relevance to the actual case for the polysilanes.

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